

# Concurrent Double-Ended Priority Queues

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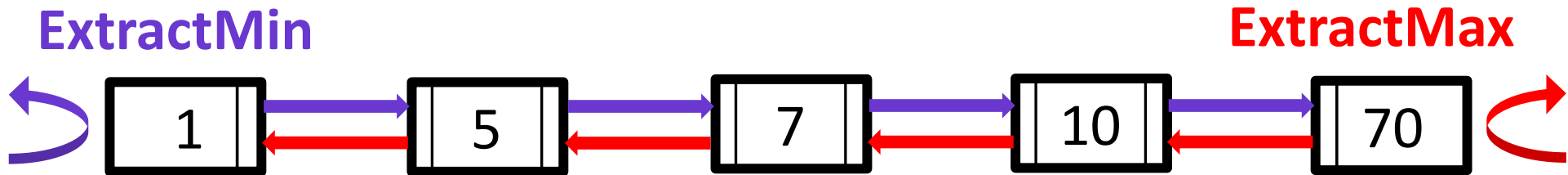
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# Double Ended Priority Queues (DEPQs)

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A DEPQ stores a set of keys and supports the following operations:

- **Insert:** Inserts an element into the set.
- **ExtractMin:** Extracts and returns the minimum element of the set.
- **ExtractMax:** Extracts and returns the maximum element of the set.



Example of concurrent DEPQ implemented as a sorted doubly-linked list.

# Applications of Priority Queues

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They have been used in the following settings:

- Operating systems
- Graph algorithms
- Event driven simulation

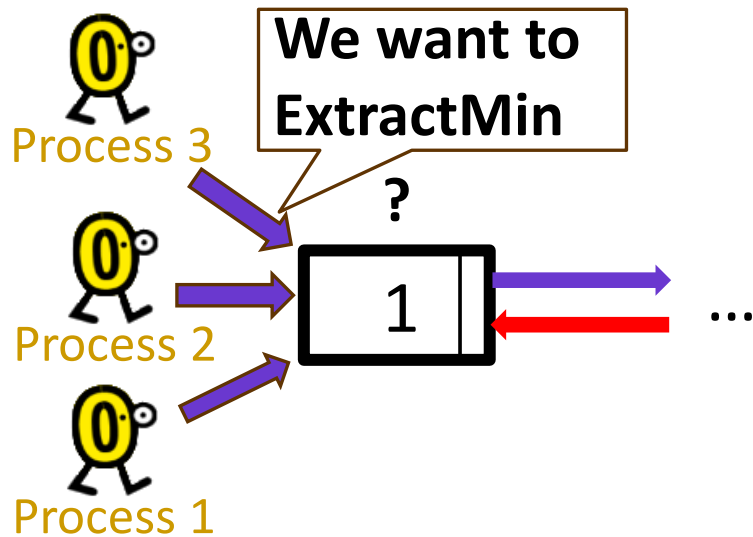
# Our Contribution

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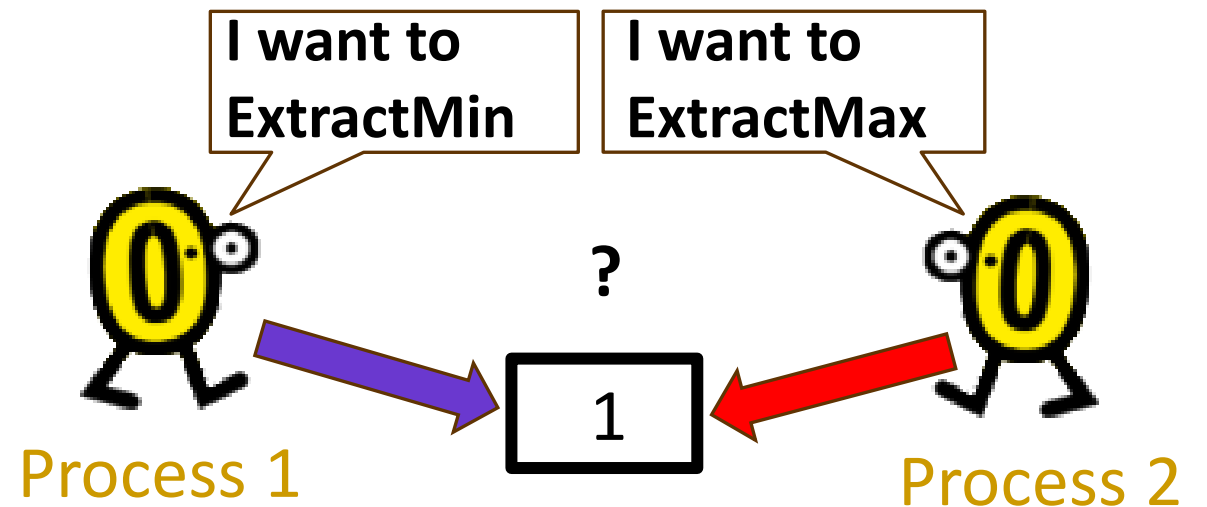
- General transformation to construct a linearizable concurrent DEPQ from a concurrent (single-ended) priority queue.
  - Insertions proceed concurrently with one another and with Extract operations.
- We use it to build the first concurrent DEPQs.
- It works even if the single-ended priority queues used are *single-consumer*, meaning that only one process at a time may perform ExtractMin operations.
- It preserves linearizability.

# Concurrent Double Ended Priority Queues

- Synchronization is required between operations that perform on the same end.



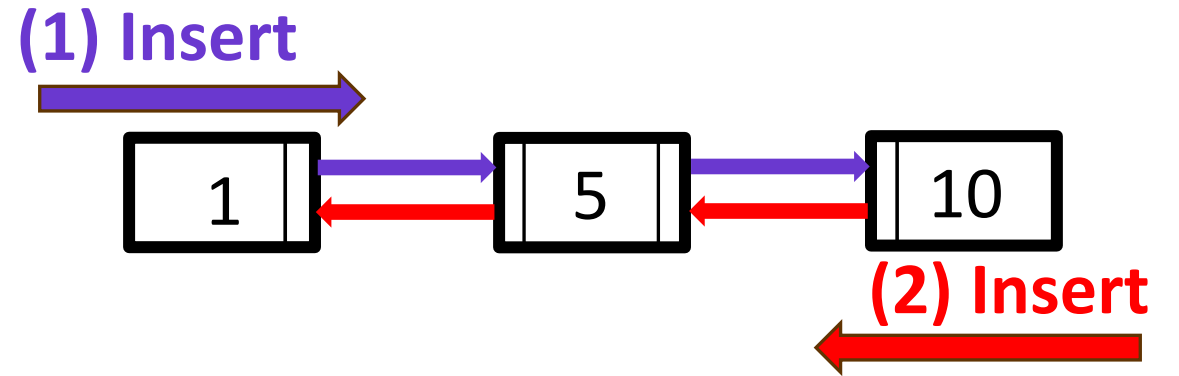
- Synchronization is required between operations that perform on different end.



# Main Ideas

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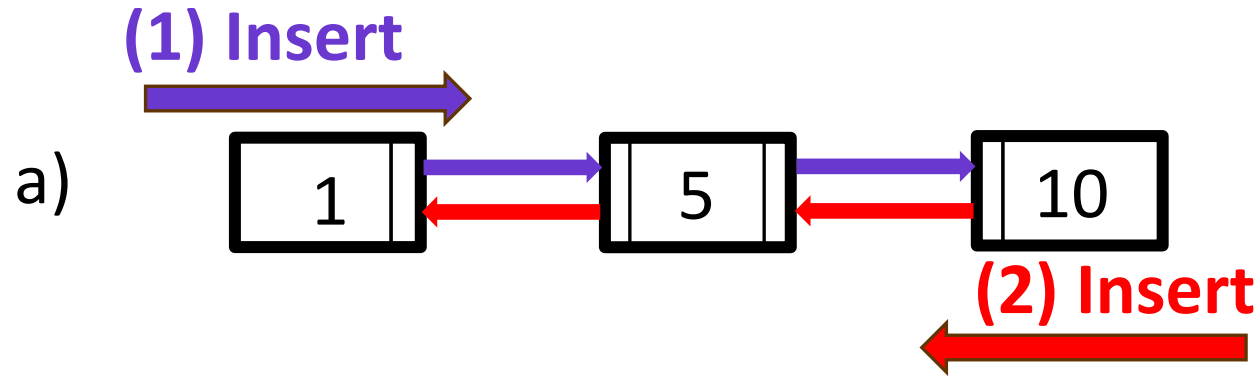
- Two Single-Ended Priority Queue instances sharing the same nodes.



Example of concurrent DEPQ implemented as two sorted single-linked list.

- Ascending order
- Descending order

# FRX Technique: Insert Operation

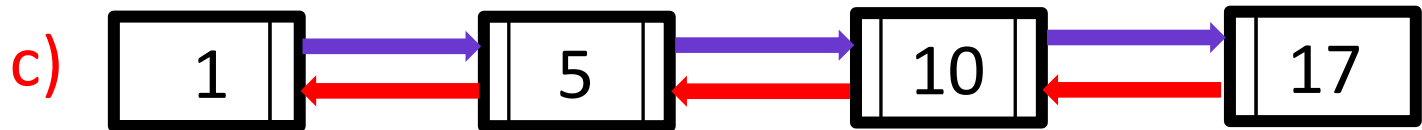
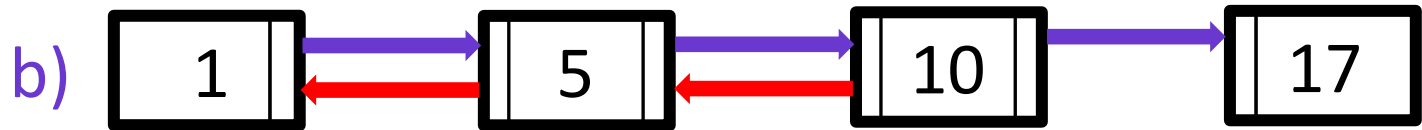


## DEPQ-Insert(e)

**Step 1:** Call Insert(e) on min single-ended priority queue.

**Step 2:** Call Insert(e) on max single-ended priority queue.

## DEPQ-Insert(17)



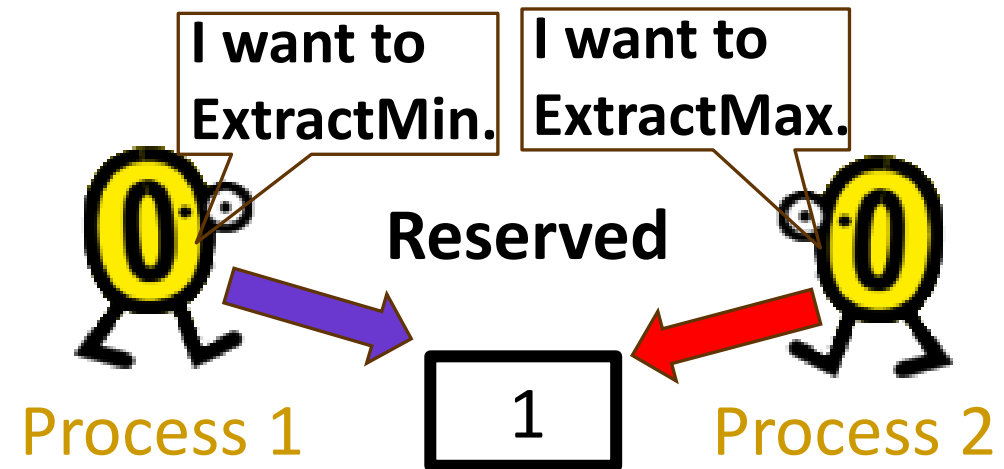
# FRX Technique: Extract Operation

Each node stores a bit, called Reserved.

## ExtractMin

- Repeatedly do the following:
  - Invoke ExtractMin on min priority queue; let  $v$  be the node returned.
  - Apply a Test&Set on the Reserved bit of  $v$ .
  - If Test&Set was successful
    - **Delete  $v$**  // if Delete is supported on single-ended PQ.
    - Return  $v.key$

ExtractMax works in a symmetric way.

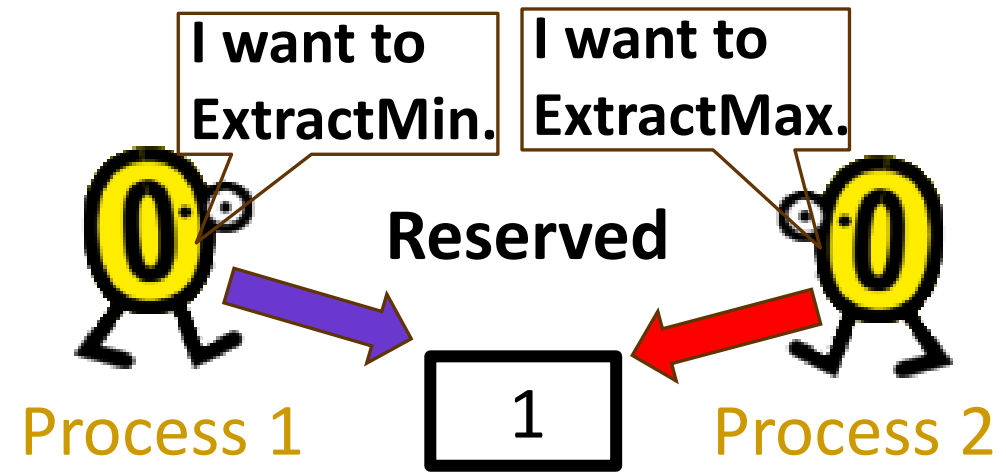


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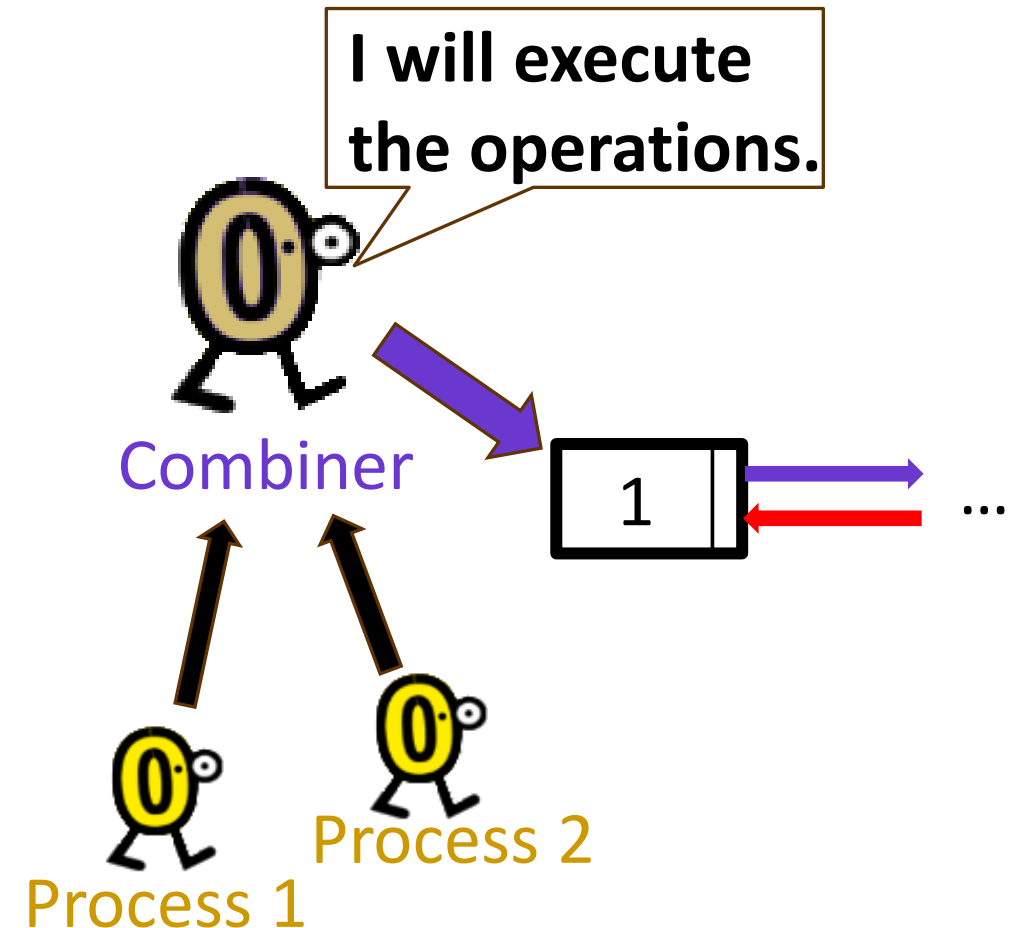


ExtractMax works in a symmetric way.

# Constructing a Multi-Consumer DEPQ from a Dual-Consumer DEPQ

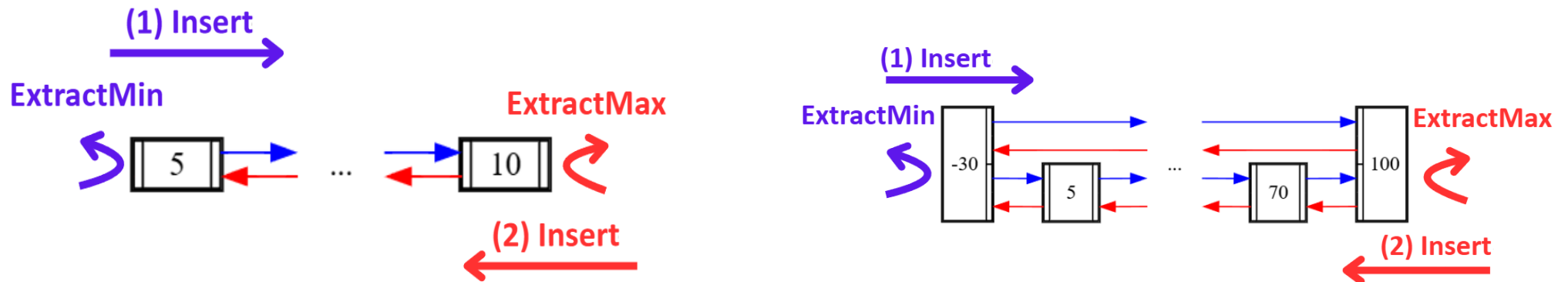
We employ CC-synch, the state-of-the-art software combining algorithm.  
[Fatourou & Kallimanis, PPOPP 2022]

- One combiner on each end that undertakes the task to execute the Extract operations invoked by the threads on that end.



# Conclusion

- General transformation to construct linearizable concurrent DEPQs from concurrent single-ended PQs.
- We utilize the construction to get the first concurrent DEPQs.
- Recent experimental work shows that applying the technique to various existing single-ended priority queues constructs fast linearizable concurrent DEPQs.



# Thank you!



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# Constructing a Multi-Consumer DEPQ from a Dual-Consumer DEPQ

We employ CC-synch, the state-of-the-art software combining algorithm. [Fatourou & Kallimanis, PPOPP 2022]

## Main Ideas in Software Combining

- Processes first announce their synchronization requests by e.g., writing a function pointer in a shared variable.
- Processes synchronize with one another to choose a combiner process, which serves in addition to its own request, active requests by other processes.
- Processes that do not become combiners perform local spinning until the combiner informs them that it has performed their requests.

